



**SUMMER – 15 EXAMINATIONS**

**Subject Code: 17204**

**Model Answer-Engineering Mechanics**

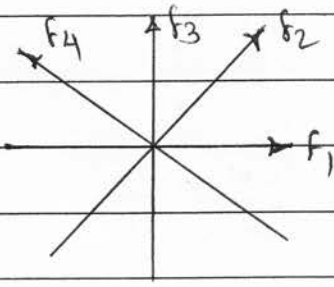
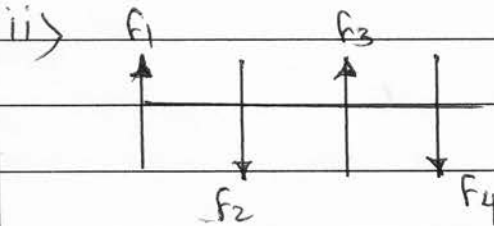
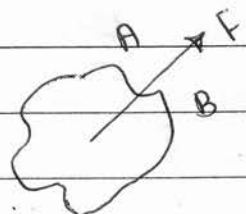
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**Important Instruction to Examiners:-**

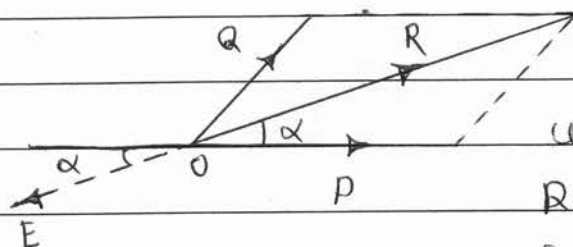
- 1) The answers should be examined by key words & not as word to word as given in the model answers scheme.
- 2) The model answers & answers written by the candidate may vary but the examiner may try to access the understanding level of the candidate.
- 3) The language errors such as grammatical, spelling errors should not be given more importance.
- 4) While assessing figures, examiners, may give credit for principle components indicated in the figure.
- 5) The figures drawn by candidate & model answer may vary. The examiner may give credit for any equivalent figure drawn.
- 5) Credit may be given step wise for numerical problems. In some cases, the assumed contact values may vary and there may be some difference in the candidate's answers and model answer.
- 6) In case of some questions credit may be given by judgment on part of examiner of relevant answer based on candidates understanding.
- 7) For programming language papers, credit may be given to any other programme based on equivalent concept.

**Important notes to examiner**

Q.NO	SOLUTION	MARKS
Q-1 (a)	i) Mechanical Advantage (M.A) The ratio of load lifted to the corresponding effort applied for a machine called Mechanical advantage.	01 M
	ii) Velocity ratio (V.R) The ratio of distance travelled by effort to corresponding distance travelled by load known as velocity ratio	01 M
b)	characteristics of an ideal machine: i) A machine whose efficiency exactly equal to 100%. ii) Input should be equal to output iii) Velocity ratio should be equal to mechanical advantage	02 M (1 M each write any two)
c)	i) Input: The work done by the effort is known as input to the machine. Since work done by a force is defined as product of force & distance moved in direction of force	01 M
	ii) Output: it is defined as useful work got out of machine i.e. work done by load.	01 M

Q.NO	SOLUTION	MARKS
d)	Concurrent force system	Non-concurrent force system
i)	This system in which all forces act at the same point known as concurrent forces	i) the system in which forces act at a different point known as non-concurrent forces
ii)		
e)	<p>i) Bow's notation - Bow's notation is used designate a force. As per this notation, each force is designated or named by two spaces one on each side of the line of action of a force. this space are generally named by capital letters as A, B, C ... serially</p> <p>ii) Explanation - A force say 'F' acting on rigid body divided space above or below it into two parts, say 'A' &amp; 'B' hence the force 'F' is named as AB</p> 	<p>01M (Fig) 01M 01M</p>

Q.NO	SOLUTION	MARKS
f)	characteristic of a force	
	i) <u>Magnitude</u> —	02M
	The quantity of force is known as its magnitude	(1M
	ii) <u>sense or nature</u> —	for each
	The arrow head marked according to the appli-	write
	cation of force indicate the sense or nature	any
	of force.	Two)
	iii) <u>Direction</u> —	
	The line of action along and towards which	
	the force acts is called as direction of force.	
	iv) <u>point of application</u> —	
	The point at which the force acts is known	
	as the point of application of the force.	
g)	use of funicular polygon	
	Funicular polygon is necessary to locate	
	position of the resultant of non-concurrent	02M
	forces.	

Q.NO	SOLUTION	MARKS	
h)	Resultant different from equilibrant		
	 <p style="text-align: right;">where R = Resultant E = Equilibrant</p>	0/1M for fig	
	<p style="text-align: center;"><u>Resultant (R)</u></p> <p>i) Resultant is defined as a single force which produces the same effect on body that has produced by number of forces acting on it.</p>	<p style="text-align: center;"><u>Equilibrant (E)</u></p> <p>i) Equilibrant is defined as a single force which keeps the body in equilibrium when number of forces acting on it.</p>	0/1M (0/1M for any ONE Point)
	<p>ii) Resultant causes the displacement in body</p>	<p>ii) As Equilibrant keeps the body in equilibrium condition there is no displacement.</p>	
	<p>iii) Resultant has the magnitude and direction</p>	<p>iii) Equilibrant force has the same magnitude as that resultant &amp; opposite direction to that of resultant.</p>	

Q.NO	SOLUTION	MARKS
i)	<p>i) Statement of Lami's theorem if three coplanar forces acting on body at a point kept in equilibrium, then each force proportional to sine of angle between the other two forces</p>	01 M
	<p>ii) Limitation of Lami's theorem</p> <ul style="list-style-type: none"> <li>- Not applicable for non-concurrent forces</li> <li>- Not applicable for less than three concurrent forces</li> <li>- Not applicable for more than three concurrent forces</li> <li>- Not applicable for forces if body is not in equilibrium.</li> <li>- the forces must be pull forces.</li> </ul>	01 M (0.5 M each write any Two)
j	<p>Law's of friction for static condition</p> <p>i) The direction of frictional force is opposite to that of motion</p> <p>ii) frictional force acts at the common surface of contact</p> <p>iii) The limiting value of frictional force is proportional to normal reaction</p> <p>iv) limiting friction is independent of area of contact.</p> <p>v) friction is depend on material and roughness at surface of contact.</p> <p>vi) static friction is always more than dynamic friction</p>	02 M (0.5 M each write any Two)

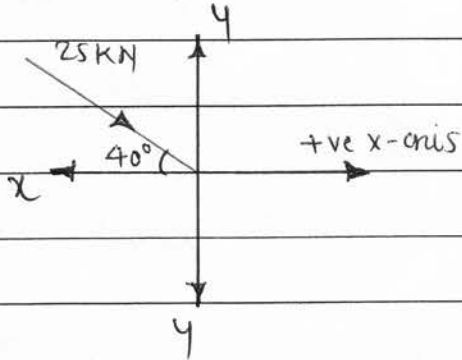
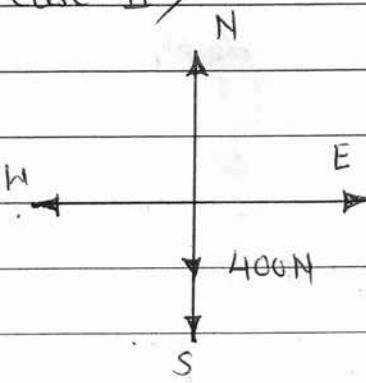


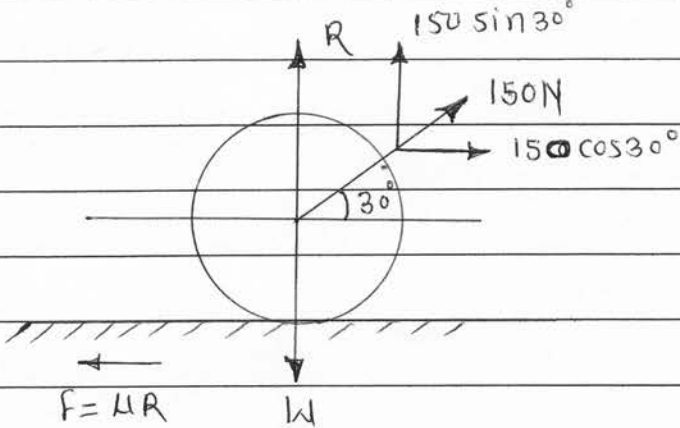
Q.NO	SOLUTION	MARKS
k)	<p>Define limiting friction                      it is the maximum value of frictional force which is held along the surface contact between two bodies when the body is just on point of motion over other known as limiting friction.</p>	02 M
l)	<p>velocity ratio worm and worm wheel</p>	
i)	<p><math>VR = \frac{RT}{r}</math> where as                      R = Radius of effort wheel                      T = number of teeth on worm wheel                      r = radius of load drum  <u>or</u></p>	<p>01 M                      (for formula)                      &amp;                      1 M                      meaning of Term's  <u>OR</u></p>
ii)	<p>if wheel handle is used</p>	
	<p><math>VR = \frac{LT}{r}</math> where                      L = Length of handle                      T = number of teeth on worm wheel</p>	<p>01 M                      for formula</p>
	<p>r = radius of load drum</p>	<p>01 M                      for meaning of Term's)</p>



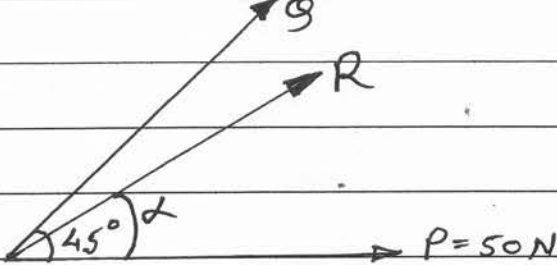


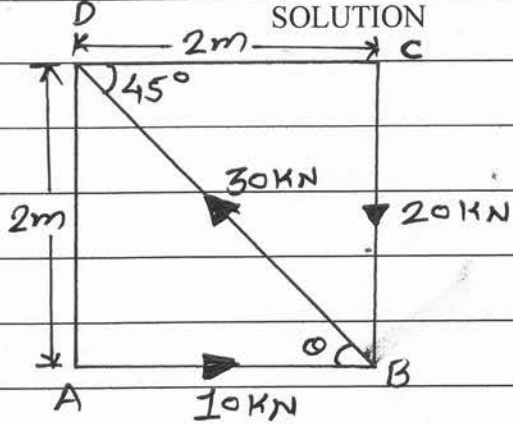
Q.NO	SOLUTION	MARKS
b)	given data :	
	$W = 1400 \text{ N}$ $D = 40 \text{ cm}$	
	$P = 40 \text{ N}$ $d_1 = 10 \text{ cm}$ $d_2 = 8 \text{ cm}$	
	i) $M.A = \frac{W}{P} = \frac{1400}{40} = 35$	01 M
	ii) $V.R = \frac{2D}{d_1 - d_2} = \frac{2 \times 40}{10 - 8} = 40$	01 M
	iii) Efficiency = $\frac{M.A}{V.R} \times 100$	
	$\eta\% = \frac{35}{40} \times 100 = 87.5\%$	
	$\eta\% = 87.5\%$	01 M
	iv) $P_f = P - \frac{W}{V.R}$	
	$P_f = 40 - \frac{1400}{40}$	
	$P_f = 5 \text{ N}$	01 M
c)	given data	
	$D = 250 \text{ mm}$ $W = 3 \text{ kN} = 3000 \text{ N}$	
	$d = 100 \text{ mm}$ $\eta\% = 80\%$	
	i) $V.R = \frac{2D}{D - d} = \frac{2 \times 250}{250 - 100} = 3.33$	01 M

Q.NO	SOLUTION	MARKS
	ii) To find effort $P'$	
	$\eta\% = \frac{M.A}{V.R} \times 100$	01M
	$\eta\% = \frac{W/P}{V.R} \times 100$	
	$80 = \frac{3000}{3.33 P} \times 100$	
	$80 = \frac{3000}{3.33 P} \times 100$	
	$P = \frac{3000 \times 100}{3.33 \times 80} \quad \therefore P = 1126.12 \text{ N}$	02M
	d) case-I	
		
	i) $\Sigma F_x = 25 \cos 40 = 19.15 \text{ kN}$	01M
	ii) $\Sigma F_y = 25 \sin 40 = -16.06 \text{ kN}$	01M
	case-II	
		
	i) $\Sigma F_x = 0$	01M
	ii) $\Sigma F_y = -400 \text{ N}$	01M

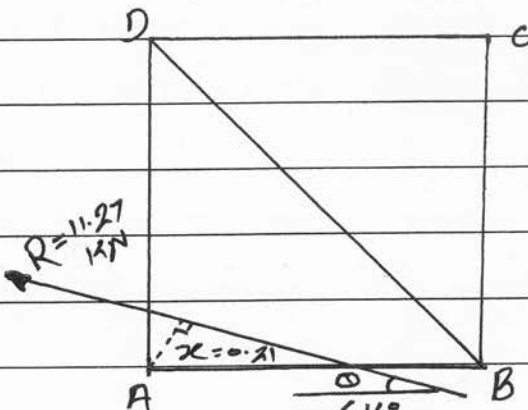
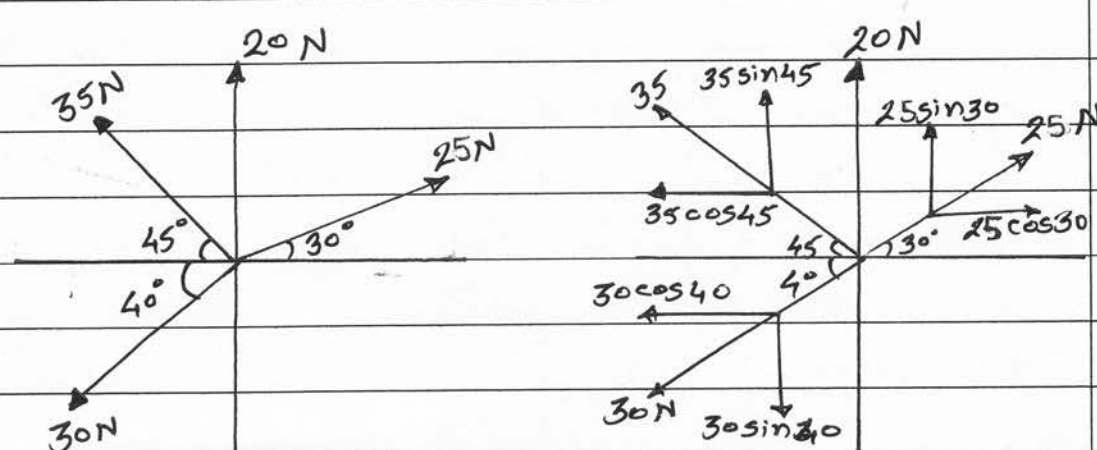
Q.NO	SOLUTION	MARKS
Q-2 (e)	 <p style="text-align: center;"><math>F = \mu R</math>      <math>W</math></p>	
	$\rightarrow \sum F_x = 0$	
	$150 \cos 30^\circ - F = 0$	0.1 M
	$150 \cos 30^\circ = F$	but $F = \mu R$
	$\boxed{129.90 \text{ N} = F}$	$\therefore R = \frac{F}{\mu} = \frac{129.90}{0.3}$
	$\sum F_y = 0$	$\boxed{R = 433 \text{ N}}$ 0.1 M
	$R - W + 150 \sin 30^\circ = 0$	
	$R + 75 - W = 0$	
	$R + 75 = W \quad \text{--- (1)}$	0.1 M
	put $R = 433$ in eq <sup>n</sup> (1)	
	$433 + 75 = W$	
	$\boxed{W = 508 \text{ N}}$	0.1 M

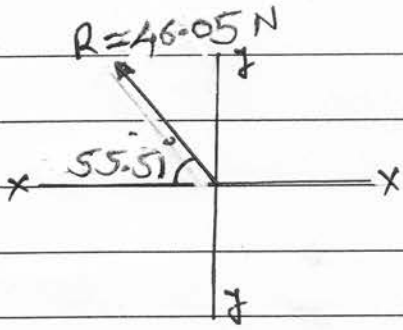
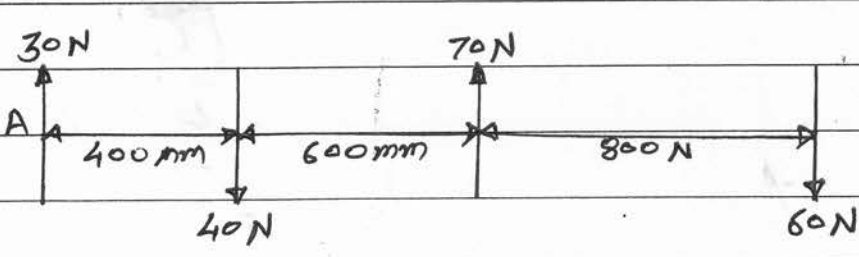
Q.NO	SOLUTION	MARKS
Q-2		
f)	properties of couple with examples	
a)		
i)	The resultant of the forces of a couple is zero.	
ii)	The moment of a couple is equal to the product of one of the forces and arm of a couple ie. $M = P \times a$	( $\frac{1}{2}$ M for each point)
iii)	Moment of a couple about any point is constant	write any <u>Four</u> )
iv)	A couple can be balanced only by another couple of equal and opposite moment	
v)	Two or more couples are said to be equal when they have same sense and moment.	
vi)	Any number of coplanar couples can be represented by a single couple, the moment of which is equal to the algebraic sum of the moments of all the couples.	
b)	examples of couple	
i)	Tap handle being rotated by a person.	( $\frac{1}{2}$ M for each example)
ii)	Key of a lock	
iii)	opening or closing the cap of a pen	
iv)	Moving the steering of a car etc.	write any <u>Four</u> )
v)	Rotation of screw cap	
vi)	winding of a watch.	
vii)	capstan being rotated by two men.	

Q.NO	SOLUTION	MARKS
Q3 a)		
	Let, $P = 50 \text{ N}$ , $Q = ?$ , $\theta = 45^\circ$ , $R = 200 \text{ N}$	
	$\therefore R = \sqrt{P^2 + Q^2 + 2PQ \cos \theta}$	1
	$200 = \sqrt{50^2 + Q^2 + 2 \times 50 \times Q \cos 45}$	
	$40000 = 2500 + Q^2 + 70.71Q$	
	$\therefore Q^2 + 70.71Q - 37500 = 0$	1
	Solve for $Q$	
	$\therefore Q = 161.495 \text{ N}$	
	Magnitude of force $Q = 161.495 \text{ N}$	1
	Let $\alpha$ be the direction of Resultant $R$ with force $P = 50 \text{ N}$	
	$\alpha = \tan^{-1} \left( \frac{Q \sin \theta}{P + Q \cos \theta} \right) =$	
	$= \tan^{-1} \left( \frac{161.495 \cdot (\sin 45)}{50 + 161.495 \cos 45} \right)$	
	$\alpha = 34.81^\circ$ w.r.to $50 \text{ N}$ force	1
	Resultant makes an angle of $34.81^\circ$ with $50 \text{ N}$ force.	

Q.NO	SOLUTION	MARKS
Q3 b)	 <p style="text-align: right;"> <math>\theta = \tan^{-1} \left( \frac{AD}{AB} \right)</math>  <math>\theta = \tan^{-1} \left( \frac{2}{2} \right)</math>  <math>\theta = 45^\circ</math> </p>	
1)	<p>Resolving forces horizontally</p> $\sum F_x = 10 - 30 \cos 45 = -11.21 \text{ KN}$	1/2
2)	<p>Resolving forces vertically</p> $\sum F_y = -20 + 30 \sin 45 = 1.21 \text{ KN}$	1/2
3)	<p>Magnitude of Resultant</p> $R = \sqrt{\sum F_x^2 + \sum F_y^2}$ $= \sqrt{(-11.21)^2 + (1.21)^2}$ $R = 11.27 \text{ KN}$ <p style="text-align: right;">             since <math>\sum F_x</math> is -ve  <math>\sum F_y</math> is +ve              R lies in second quadrant         </p>	1
4)	<p>Direction of Resultant</p> $\tan \theta = \frac{\sum F_y}{\sum F_x} = \left( \frac{1.21}{-11.21} \right) = 0.1079$ $\therefore \theta = \tan^{-1}(0.1079) = 6.16^\circ \text{ with horizontal}$	1
5)	<p>Position of Resultant w.r. to. A</p> <p>Taking moment about point A</p> $\sum M_A = (10 \times 0) + (20 \times 2) - (30 \sin 45 \times 2)$ $\sum M_A = -2.426 \text{ KN.m} \dots (\text{Anticlockwise})$	



Q.NO	SOLUTION	MARKS
Q3 b) Cont....	Applying Varignon's theorem $\sum M_A = R \times x$	
	$2.426 = 11.27 \cdot x$	
	$\therefore x = 0.215 \text{ m}$	1M
	Position of Resultant lie at a perpendicular distance of 0.215 m w.r. to point A.	
		
Q3 c)		
	1) Resolving force System horizontally	
	$\sum F_x = 25 \cos 30 - 35 \cos 45 - 30 \cos 40$	
	$\sum F_x = -26.079 \text{ N}$	
	$\boxed{F_x = -26.079 \text{ N}}$	0.1M

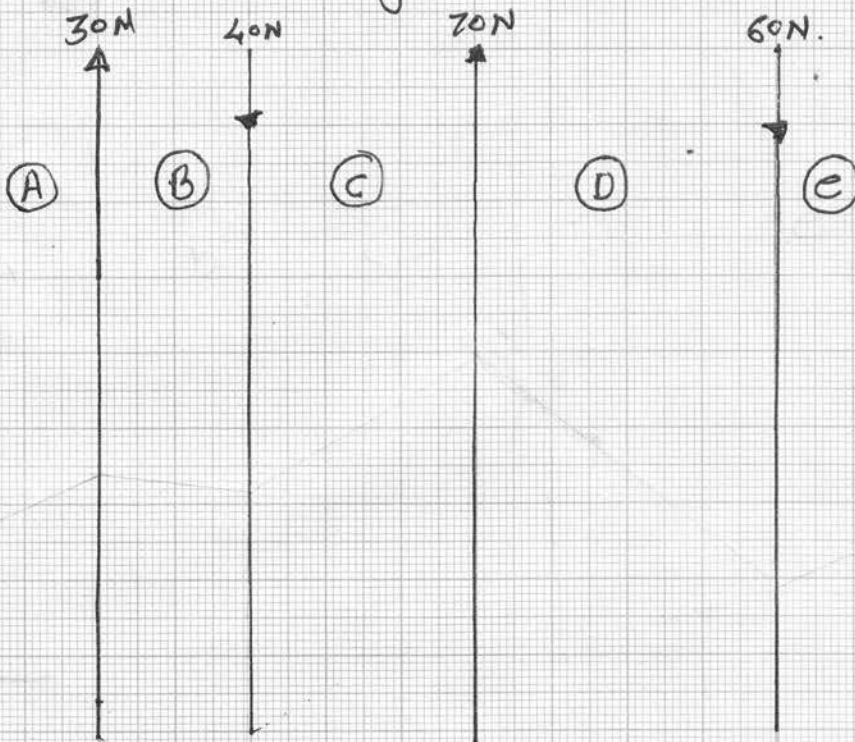
Q.NO	SOLUTION	MARKS
Q3 c) Cont...	27 Resolving force system vertically. $\sum F_y = 25 \sin 30 + 20 + 35 \sin 45 - 30 \sin 40$ $\sum F_y = 37.96 \text{ N}$	1
	37 Resultant $R = \sqrt{(\sum F_x)^2 + (\sum F_y)^2}$ $R = \sqrt{(-26.079)^2 + (37.96)^2}$ $R = 46.05 \text{ N}$	1
	47 Angle of Inclination of Resultant $\theta = \tan^{-1} \left( \frac{\sum F_y}{\sum F_x} \right)$ $= \tan^{-1} \left( \frac{37.96}{26.079} \right)$	
	$\theta = 55.51^\circ$	1
	since $\sum F_x$ is negative & $\sum F_y$ is positive. Resultant lie in the second quadrant	
		
Q3 d)		

Q. NO	SOLUTION	MARKS
Q3d Cont....	<p>i) Magnitude of Resultant (R)</p> $R = \sum F_y$ $= 30 - 40 + 70 - 60$ $R = 0 \text{ N.}$	2M
*	<p>NOTE</p> <p>As the magnitude of Resultant is zero the force system is in equilibrium.</p> <p>Hence there is no position &amp; direction of Resultant force.</p>	2M
Q3e)	<p>i) Resolution of a force</p> <p>The way of representing a single force into number of forces without changing the effect of the force on the body is called as Resolution of a force.</p> <p>Suppose a single force <math>F</math> is to be resolved into number of forces <math>F_1, F_2, F_3, F_4 \dots</math> etc.</p> <p>then these number of forces are called as Components of a single force <math>F</math>.</p>	02
	<p>ii) Composition of a force system</p> <p>The process of finding out the resultant force of a given system of forces is called as Composition of forces.</p> <p>The single force <math>F</math> is called resultant force of forces <math>F_1, F_2, F_3, F_4 \dots</math> etc.</p>	02

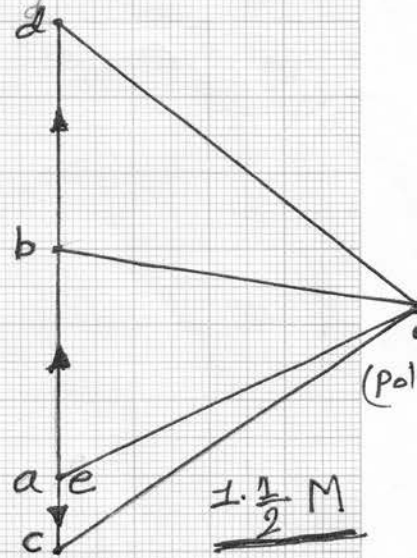
Q NO	SOLUTION	MARKS
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Q37

space diagram (scale 1cm = 200mm)



$1 \frac{1}{2} M$  for space diagram.



Vector diagram & polar diagram  
(scale 1cm = 10 N)

i) Magnitude of Resultant = length ae  $\times$  scale  
 $= 0 \times 10$

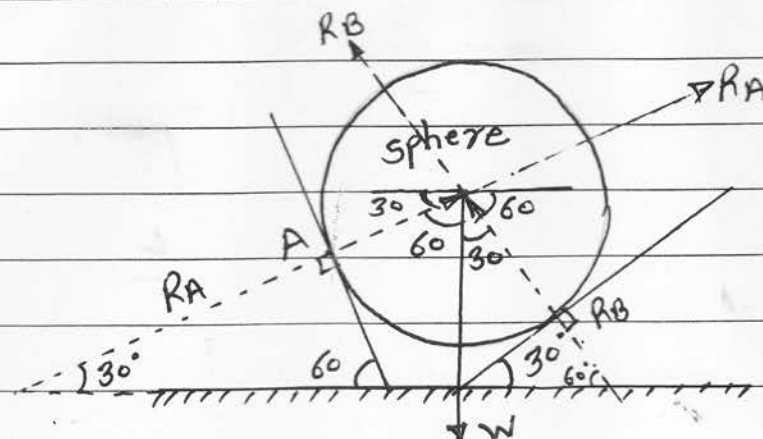
R. = 0 N.

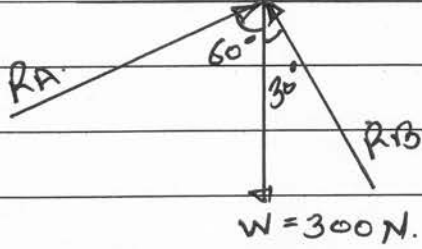
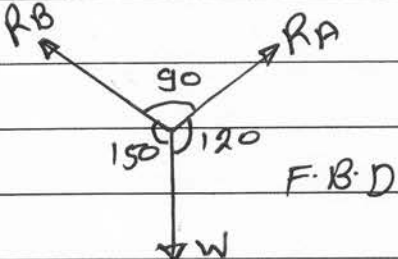
NOTE:-

As the magnitude of Resultant is zero the force system is in equilibrium. Hence there is no position & direction of resultant force.

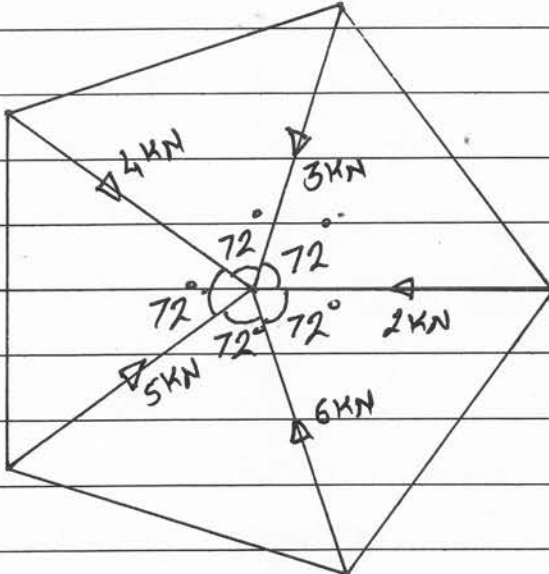
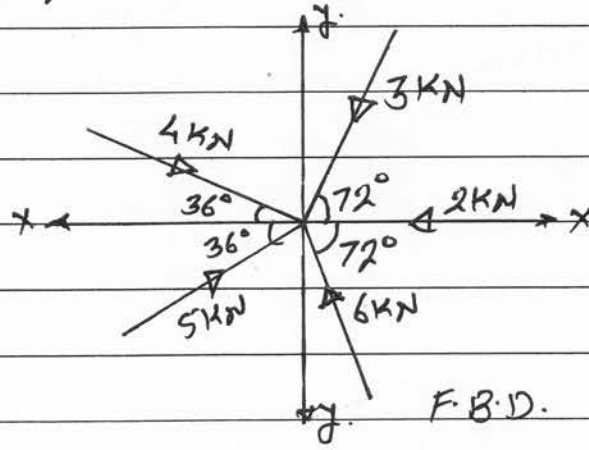
1M

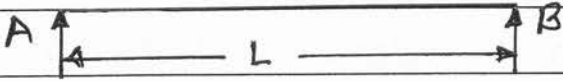
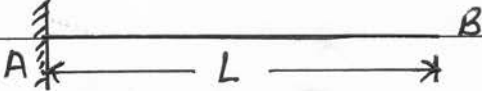


Q.NO	SOLUTION	MARKS
Q4 a)	<p>i) Graphical Condition of equilibrium for Concurrent system.</p> <p>The resultant of Coplanar Concurrent forces is found by joining the beginning of the first force to the end of the last force in the force polygon. If the system of forces is in equilibrium, the resultant must be zero. Thus for the system to be in equilibrium the polygon of forces must be a closed figure.</p>	02
	<p>ii) Graphical Condition of equilibrium for parallel force system.</p>	
	<p>a) The system of forces to be in equilibrium the force polygon must be a closed figure.</p>	1M
	<p>b) The system of forces to be in equilibrium the funicular polygon must be a closed figure.</p>	1M
Q4 b)	 <p>The diagram shows a sphere on an inclined plane. A vertical line represents the weight <math>W</math> acting downwards from the center. A reaction force <math>R_A</math> acts perpendicular to the inclined plane at point A. Another reaction force <math>R_B</math> acts perpendicular to the inclined plane at point B. The angle of the inclined plane with the horizontal is <math>30^\circ</math>. The weight <math>W</math> is shown to be bisected by a vertical line, with <math>30^\circ</math> angles marked between the vertical line and the weight vector. The reaction forces <math>R_A</math> and <math>R_B</math> are shown to be perpendicular to the inclined plane, with <math>60^\circ</math> angles marked between the vertical line and these reaction forces.</p>	

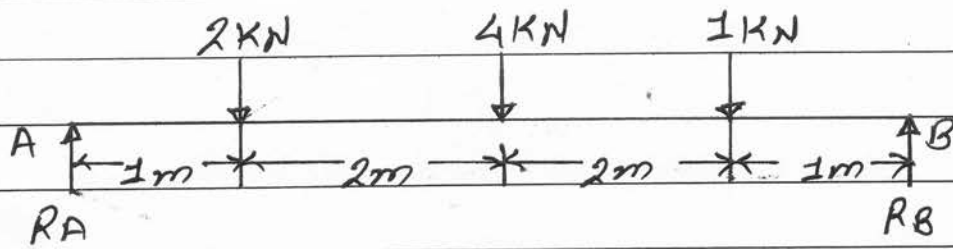
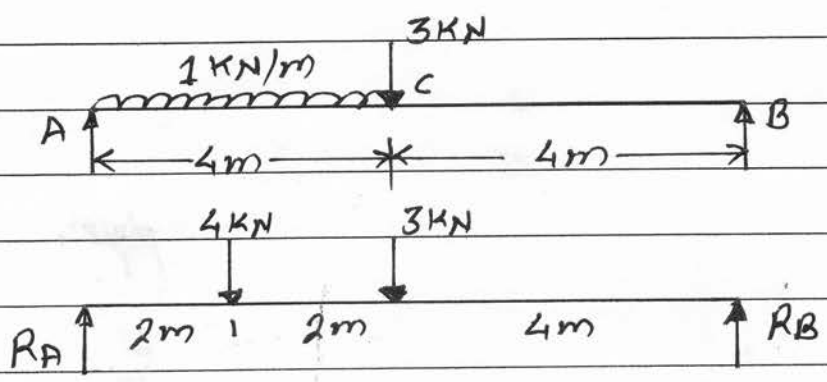
Q.NO	SOLUTION	MARKS
94b		
Cont...		
		1
	F.B.D	
	Applying Lami's Theorem	
	$\frac{R_A}{\sin 30} = \frac{R_B}{\sin 60} = \frac{W}{\sin(60+30)}$	1
	$\therefore R_A = \frac{W \cdot \sin 30}{\sin 90} = 150 \text{ N.}$	1
	$\therefore R_B = \frac{W \sin 60}{\sin 90} = 259.80 \text{ N}$	1
	<u>OR</u>	
94b		
		1
	F.B.D	
	Apply Lami's Theorem	
	$\frac{R_A}{\sin 150} = \frac{R_B}{\sin 120} = \frac{W}{\sin 90}$	1
	$\therefore R_A = \frac{W \sin 150}{\sin 90} = 150 \text{ N}$	1
	$\therefore R_B = \frac{W \sin 120}{\sin 90} = 259.80 \text{ N}$	1



Q.NO	SOLUTION	MARKS
Q4c)		
<p>For regular pentagon the angles between each pair of forces = <math>\frac{360}{5} = 72^\circ</math></p>		
 <p style="text-align: center;">F.B.D.</p>		
<p>1) Resolving all the forces horizontally</p>		
$\sum F_x = -2 - 3\cos 72 - 6\cos 72 + 4\cos 36 + 5\cos 36$		
$\sum F_x = 2.5 \text{ KN}$		1
<p>2) Resolving all the forces vertically</p>		
$\sum F_y = -3\sin 72 + 6\sin 72 - 4\sin 36 + 5\sin 36$		
$\sum F_y = 3.44 \text{ KN}$		1

Q.NO	SOLUTION	MARKS
Q4 c) Cont...	37 Magnitude of Resultant	
	$R = \sqrt{(\sum F_x)^2 + (\sum F_y)^2}$ $R = \sqrt{(2.5)^2 + (3.44)^2}$ $R = 4.25 \text{ KN}$	1
	<p>Since <math>\sum F_x</math> &amp; <math>\sum F_y</math> are positive, <math>R</math> is pull in the first quadrant. So Equilibrant <math>E</math> is pull in the third quadrant.</p> $E = R = 4.25 \text{ KN.}$	1
Q4 d)	<p>i) simply supported beam</p> <p>A beam which is freely supported on the walls or columns at its both the ends is called as a simply supported beam.</p> 	
	<p>ii) Cantilever beam</p> <p>A beam fixed at one end and free at other is called as a Cantilever beam.</p> 	1
	<p>iii) Overhanging beam</p> <p>If the end portion of the beam extends beyond the supports it is called as an overhanging beam. A beam may be overhanging on one side or both sides.</p>	

Q.NO	SOLUTION	MARKS
94d) Cont...		
	<p>overhung on right side</p> <p>overhung on both sides</p> <p>overhung on left side</p>	1
	<p>iv) Fixed beam</p> <p>A beam whose both the ends are rigidly fixed in walls is called a fixed beam, Constrained beam, built-in beam or an encastré beam.</p>	1
	<p>v) Continuous beam</p> <p>A beam which is supported on more than two supports is called a Continuous beam.</p>	
	<p>Two span Continuous beam.</p>	1
	<p>Three span Continuous beam.</p>	

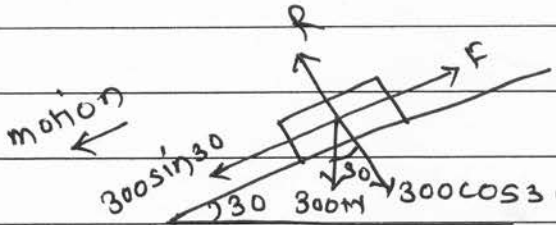
Q.NO	SOLUTION	MARKS
Q4 e)	 <p> <math>\rightarrow</math> Applying Condition of equilibrium  <math>\sum F_y = 0</math>  <math>R_A - 2 - 4 - 1 + R_B = 0</math>  <math>R_A + R_B = 7 \text{ kN.} \dots\dots (i)</math> </p>	
	$\sum M @ A = 0$ $(2 \times 1) + (4 \times 3) + (1 \times 5) - R_B \times 6 = 0$ $2 + 12 + 5 = 6 R_B$ $\therefore R_B = 3.17 \text{ kN}$	1M
	<p>from eq<sup>n</sup> (i)</p> $R_A + R_B = 7$ $\therefore R_A = 7 - 3.17 = 3.83 \text{ kN}$	1M
	<div style="border: 1px solid black; padding: 5px; display: inline-block;">           Ans. <math>R_A = 3.83 \text{ kN}</math>  <math>R_B = 3.17 \text{ kN}</math> </div>	
Q4 f)		

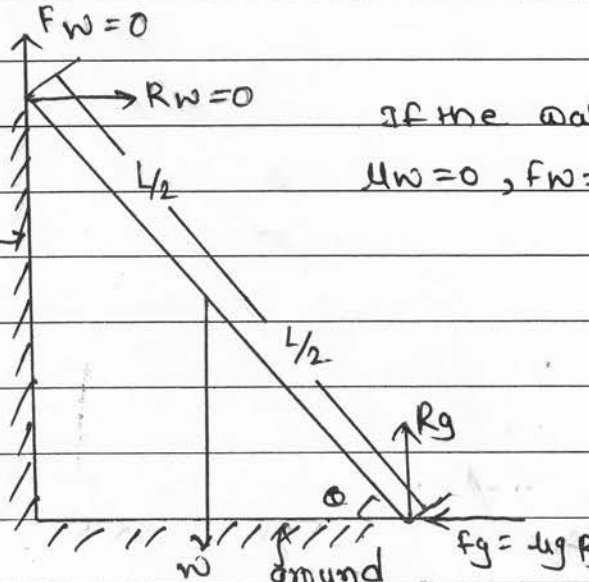


Q.NO	SOLUTION	MARKS
Q.5	Answer any four of the following	
9)	Given data: - $w = 400\text{ N}$ , $P = 120\text{ N}$ , $\theta = 30^\circ$	
	Find: 1) coefficient of friction ( $\mu$ ) 2) Normal reaction ( $R$ )	
		01
	3] Resolve the forces horizontally, we get $\Sigma F_x = 120 \cos 30 - F$ $\Sigma F_x = 103.92 - \mu R$ ( $\because F = \mu R$ )	
	As the body is in limiting equilibrium, $\Sigma F_x = 0$ $\therefore 103.92 - \mu R = 0$ $103.92 = \mu R$ $\mu = \frac{103.92}{R} \rightarrow (1)$	01
	4] Resolving the forces vertically, we get $\Sigma F_y = R - w + 120 \sin 30$ $\Sigma F_y = R - 400 + 60$ $\Sigma F_y = 0$ $R - 340 = 0$ <u><math>R = 340\text{ N}</math></u>	01
	Put the value of 'R' in eq. (1), we get	



Q.NO	SOLUTION	MARKS
0.5 a. continue ----	$\mu = \frac{103.92}{366}$	
	$\mu = 0.305$	01
b)	Given data:- $w = 200\text{ N}$ , $P = 65\text{ N}$ Find:- i) $\mu$ , ii) $S$ , iii) $\phi$	
	<p>i) <math>\sum F_x = 0</math></p> $P - F = 0$ $65 - \mu R = 0 \quad (\because F = \mu R)$ $65 = \mu R$ $\mu = \frac{65}{R} \quad \text{--- (1)}$	
	<p>ii) <math>\sum F_y = 0</math></p> $R - w = 0$ $R = 200\text{ N}$	01
	<p>put the value of 'R' in eq<sup>n</sup> (1), we get</p> $\mu = \frac{65}{200}$	
	$\mu = 0.325$	01

Q.NO	SOLUTION	MARKS
Q.5b continue--	<p>III) calculate magnitude of resultant reaction</p>	
	$S = R \sqrt{1 + \mu^2}$	
	$S = 200 \sqrt{1 + (0.325)^2}$	
	$S = 210.297 \text{ N} \quad \text{---} \rightarrow \text{Resultant}$	01
	<p>IV) direction:</p>	
	$\tan \phi = \mu$	
	$\phi = \tan^{-1}(\mu)$	
	$= \tan^{-1}(0.325)$	
	$\phi = 18^\circ \quad \text{---} \rightarrow \text{direction}$	01
C]	<p>Given:</p>	
	$W = 300 \text{ N}$	
	<p>Find: i) <math>\mu</math>, ii) <math>\phi</math>, iii) <math>\alpha</math></p>	
		
	<p>I] <math>\sum F_x = 0</math></p>	
	$F - 300 \sin 30$	
	$F = 150 \text{ N}$	
	$\mu R = 150 \text{ N} \quad (\because F = \mu R)$	1/2
	$\mu = 150/R \quad \text{---} \rightarrow (1)$	

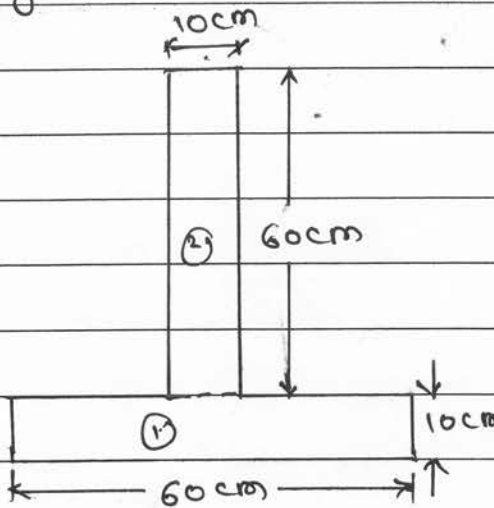
Q.NO	SOLUTION	MARKS
Q.5c	II) $\Sigma F_x = 0$	
cont.....	$R - 300 \cos 30 = 0$	
	$R = 259.807 \text{ N}$	01
	put 'R' in eqn (1)	
	$\therefore \mu = \frac{150}{259.807}$	
	$\mu = 0.577$	01
	III) $\tan \phi = \mu$	
	$\phi = \tan^{-1}(\mu)$	
	$= \tan^{-1}(0.577)$	01
	$\phi = 29.98 \text{ say } 30^\circ$	
	IV) Angle of friction = Angle of repose	
	$\phi = \alpha$	
	$\alpha = 30^\circ$	01
d]	 <p>if the wall is smooth  <math>\mu_w = 0, F_w = 0</math></p>	04

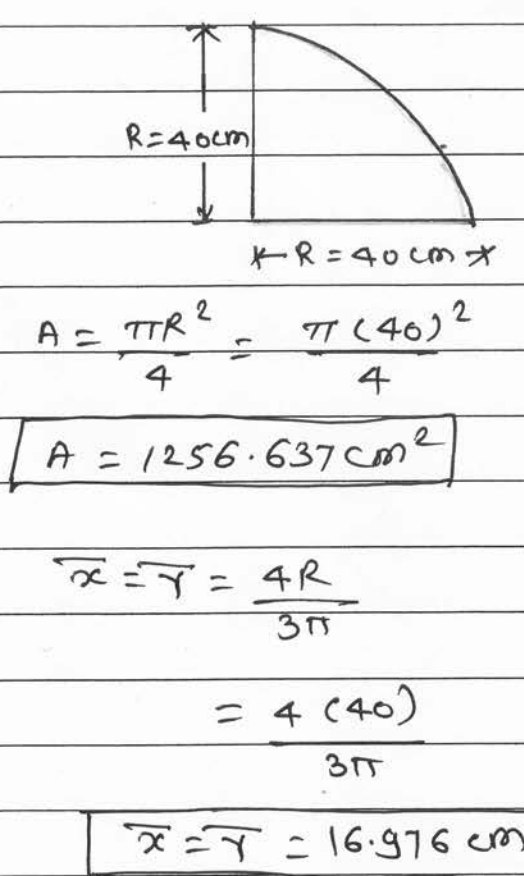
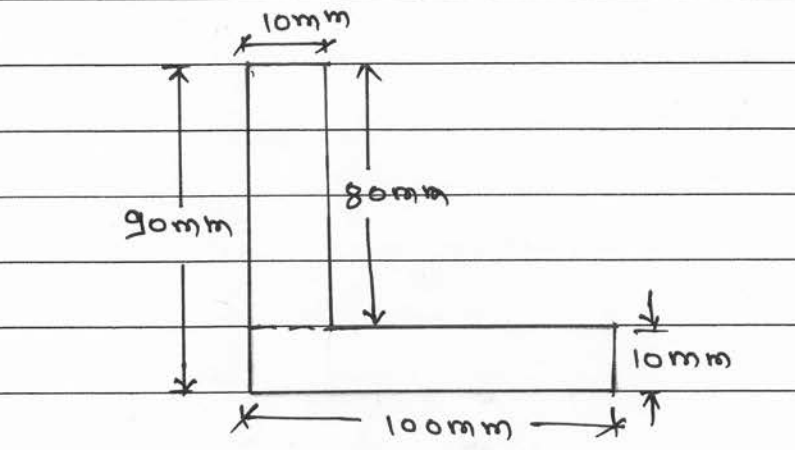
Q.NO	SOLUTION	MARKS
e]	Given:	
	$V \cdot R = 20$ ,	
	$w_1 = 100 \text{ N}$ , $P_1 = 10 \text{ N}$	
	$w_2 = 200 \text{ N}$ , $P_2 = 14 \text{ N}$	
	Find:- 1) Law of machine,	
	2) Effort lost in friction at a load of	
	300 N.	
	2] The eq <sup>n</sup> is given by	
	$P = mw + c$	
	$\therefore P_1 = mw_1 + c$	
	$10 = m(100) + c \rightarrow (i)$	
	$P_2 = mw_2 + c$	
	$14 = 200m + c \rightarrow (ii)$	
	solve eq <sup>n</sup> (i) & (ii) simultaneously	
	$10 = 100m + c$	
	$+ 14 = 200m + c$	
	$\underline{-4 = -100m}$	
	$\therefore \boxed{m = 0.04}$	1/2
	put $m$ in eq <sup>n</sup> (i), we get	
	$10 = 0.04(100) + c$	
	$10 = 4 + c$	
	$\therefore c = 10 - 4$	
	$\boxed{c = 6}$	1/2
	$\therefore \boxed{P = 0.04w + 6} \rightarrow$ Law of machine,	01

Q.NO	SOLUTION	MARKS
Q.5e	ii] $w = 300 \text{ N}$	
Cont....	$\therefore P = 0.04(300) + 6$	
	$P = 18 \text{ N}$	01
	iii] Effort lost in friction:	
	$P_f = P - P_i$	
	but, $P_i = \frac{w}{VR} = \frac{300}{20} = 15$	
	$\therefore P_f = 18 - 15$	
	$P_f = 3 \text{ N}$	01
f]	Given:-	
	$P = 50 \text{ N}, \eta = 70\%$	
	$N_1 = 60, N_2 = 10$	
	$N_3 = 90, N_4 = 15$	
	Find:- $w = ?$	
	I) $V.R. = \frac{N_1}{N_2} \times \frac{N_3}{N_4}$	01
	$= \frac{100}{25} = \frac{60}{10} \times \frac{90}{15}$	
	$V.R. = 36$	01
	II) $M.A. = \frac{w}{P} \rightarrow (1)$	
	$\eta = \frac{MA}{VR} \times 100$	01
	$70 = \frac{MA}{36} \times 100$	





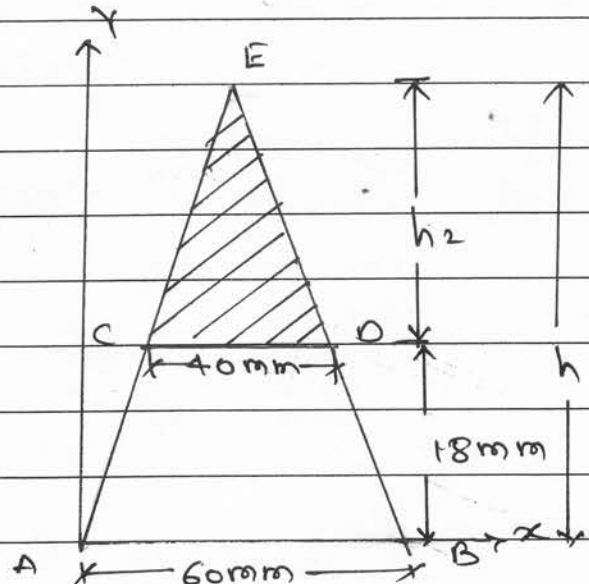
Q.NO	SOLUTION	MARKS
9.6	Attempt any four of the following	
a)		
	i) $a_1 = 60 \times 10 = 600 \text{ cm}^2$	
	$a_2 = 60 \times 10 = 600 \text{ cm}^2$	01
	ii) due to symmetry about $y-y$ axis	
	$\bar{x} = \frac{60}{2} = 30 \text{ cm}$	
	$\boxed{\bar{x} = 30 \text{ cm}}$	1/2
	iii) $y_1 = \frac{10}{2} = 5 \text{ cm}$	
	$y_2 = 10 + \frac{60}{2} = 40 \text{ cm}$	1/2
	$\bar{y} = \frac{a_1 y_1 + a_2 y_2}{a_1 + a_2}$	01
	$= \frac{(600 \times 5) + (600 \times 40)}{(600 + 600)}$	
	$\boxed{\bar{y} = 22.5 \text{ cm}}$	01

Q.NO	SOLUTION	MARKS
b]	 <p> <math>R = 40 \text{ cm}</math>  <math>R = 40 \text{ cm}</math>  <math>A = \frac{\pi R^2}{4} = \frac{\pi (40)^2}{4}</math>  <math>A = 1256.637 \text{ cm}^2</math>  <math>\bar{x} = \bar{y} = \frac{4R}{3\pi}</math>  <math>= \frac{4(40)}{3\pi}</math>  <math>\bar{x} = \bar{y} = 16.976 \text{ cm}</math> </p>	<p>02</p> <p>01</p> <p>01</p>
c]	 <p> <math>100 \text{ mm}</math>  <math>100 \text{ mm}</math>  <math>80 \text{ mm}</math>  <math>90 \text{ mm}</math>  <math>80 \text{ mm}</math>  <math>100 \text{ mm}</math>  <math>10 \text{ mm}</math> </p> <p>             I) <math>a_1 = 80 \times 10 = 800 \text{ mm}^2</math>  <math>a_2 = 100 \times 10 = 1000 \text{ mm}^2</math>              II) <math>x_1 = \frac{10}{2} = 5 \text{ mm}</math>      <math>x_1 = 5 \text{ mm}</math>  <math>x_2 = \frac{100}{2} = 50 \text{ mm}</math>      <math>x_2 = 50 \text{ mm}</math> </p>	<p>01</p>

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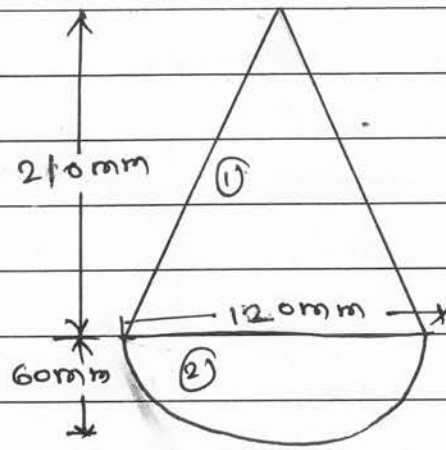
Q.NO	SOLUTION	MARKS
Q.6c cont....	$Y_1 = 10 + \frac{80}{2} = 10 + 40 = 50 \text{ mm}$	
	$Y_2 = \frac{10}{2} = 5 \text{ mm}$	0/
	$\bar{x}_1 = \frac{a_1 x_1 + a_2 x_2}{a_1 + a_2}$	
	$= \frac{(800 \times 5) + (1000 \times 50)}{(800 + 1000)}$	6/
	$\bar{x} = 30 \text{ mm}$	
	$\bar{Y} = \frac{a_1 Y_1 + a_2 Y_2}{a_1 + a_2}$	
	$= \frac{(800 \times 50) + (1000 \times 5)}{(800 + 1000)}$	
	$\bar{Y} = 25 \text{ mm}$	6/
d]	<p>The diagram shows a composite shape with a semi-circular top and a rectangular bottom. The semi-circle has a radius of 50 mm and a diameter of 100 mm. The rectangle has a height of 120 mm. The total height is 170 mm. The x-axis is horizontal and the y-axis is vertical, both originating from the bottom-left corner of the rectangle. The semi-circle is labeled (2) and the rectangle is labeled (1).</p>	
	$V_1 = \pi R^2 h$	0/
	$= \pi (50)^2 (120)$	

Q.NO	SOLUTION	MARKS
Q.6d		
cont.....	$V_1 = 942.477 \times 10^3 \text{ mm}^3$	
	$V_2 = \frac{2}{3} \pi R^3$	01
	$= \frac{2}{3} \pi (50)^3$	
	$V_2 = 261.799 \times 10^3 \text{ mm}^3$	
	<p>ii) Due to symmetry about Y-Y axis</p>	
	$\bar{x} = \frac{100}{2}$	
	$\bar{x} = 50 \text{ mm}$	01
	<p>iii) <math>d_1 = \frac{120}{2} = 60 \text{ mm}</math></p>	
	$d_2 = 120 + \frac{3R}{8}$	
	$= 120 + \frac{3(50)}{8}$	
	$d_2 = 138.75 \text{ mm}$	01/2
	$\bar{y} = \frac{V_1 \bar{y}_1 + V_2 \bar{y}_2}{V_1 + V_2} = \frac{942.477 \times 10^3 \times 60 + 261.799 \times 10^3 \times 138.75}{(942.477 \times 10^3) + (261.799 \times 10^3)}$	
	$\bar{y} = 77.12 \text{ mm}$	01/2

Q.NO	SOLUTION	MARKS
eJ		1/2
	<p>1) Fig. is symmetrical about y-y axis</p> $\bar{x} = \frac{60}{2} =$ $\boxed{\bar{x} = 30 \text{ mm}}$	1/2
	<p>h - height of full cone,  <math>h_1 =</math> height of frustum, = 18 mm  <math>h_2 =</math> height of cut cone          As the triangles <math>\Delta ABE</math> &amp; <math>\Delta CDE</math> are symmetrical</p> $\frac{h}{60} = \frac{h_2}{40}$ $h = \frac{60}{40} \times h_2$ $h = 1.5h_2$ <p>Now, <math>h_1 + h_2 = h</math> i.e. <math>h_1 + h_2 = 1.5h_2</math>  <math>\therefore h_1 = 1.5h_2 - h_2 = 0.5h_2</math>  <math>h_2 = \frac{h_1}{0.5} = \frac{18}{0.5}</math></p>	
	$\boxed{h_2 = 36 \text{ mm}}$	1/2

Q.NO	SOLUTION	MARKS
Q.6e	II) $R_1 = 30\text{mm}$ , $h = 54\text{mm}$	
cont.	$V_1 = \frac{1}{3} \pi R_1^2 h$	
	$= \frac{1}{3} \pi (30)^2 (54)$	
	$V_1 = 50.86 \times 10^3 \text{mm}^3$	
		1/2
	$V_2 = \frac{1}{3} \pi R_2^2 h_2$	
	$= \frac{1}{3} \pi (20)^2 (36)$	
	$V_2 = 15.07 \times 10^3 \text{mm}^3$	
	$\therefore$ Volume of frustum of cone	
	$V = V_1 - V_2$	
	$= (50.86 \times 10^3) - (15.07 \times 10^3)$	
	$= 35.82 \times 10^3 \text{mm}^3$	
	III) $y_1 = \frac{54}{4} = 13.5\text{mm}$	0/
	$y_2 = 18 + \frac{36}{4} = 27\text{mm}$	
	$\bar{Y} = \frac{V_1 y_1 - V_2 y_2}{V_1 - V_2}$	
	$= \frac{(50.86 \times 10^3)(13.5) - (15.07 \times 10^3 \times 27)}{(35.82 \times 10^3)}$	
	$\bar{Y} = 7.815\text{mm}$	0/

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Q.NO	SOLUTION	MARKS
f]		1/2
	<p>i) The fig. is symmetrical about Y-Y axis</p> $\bar{x} = \frac{120}{2}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 0 auto;"><math>\bar{x} = 60 \text{ mm}</math></div>	1/2
	<p>ii) <math>V_1 = \frac{1}{3} \pi R^2 h</math></p> $= \frac{1}{3} \pi (60)^2 (210)$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 0 auto;"><math>V_1 = 791.68 \times 10^3 \text{ mm}^3</math></div>	1/2
	$V_2 = \frac{2}{3} \pi R^3$ $= \frac{2}{3} \pi (60)^3$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 0 auto;"><math>V_2 = 452.389 \times 10^3 \text{ mm}^3</math></div>	
	$\bar{y}_1 = 60 + \frac{h}{4}$ $= 60 + \frac{210}{4}$ <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 0 auto;"><math>\bar{y}_1 = 112.5 \text{ mm}</math></div>	1/2



Q.NO	SOLUTION	MARKS
Q.6f	$y_2 = R - \frac{3R}{8}$	
cont....		
	$= 60 - \frac{3(60)}{8}$	1/2
	$y_2 = 37.5 \text{ mm}$	
	$\therefore \bar{Y} = \frac{V_1 y_1 + V_2 y_2}{V_1 + V_2}$	1/2
	$= \frac{(791.68 \times 10^3 \times 112.5) + (452.38 \times 10^3 \times 37.5)}{(791.68 \times 10^3) + (452.38 \times 10^3)}$	
	$\bar{Y} = 85.227 \text{ mm}$	0/